

B.A./B.Sc. 1<sup>st</sup> Semester

## QUANTITATIVE TECHNIQUES

## (Quantitative Techniques—I)

Time Allowed—3 Hours] [Maximum Marks—100

Note :— There are *eight* questions. Candidates are required to attempt any *five* questions. All questions carry equal marks.

## SECTION—A

1. (a) What are simultaneous Linear Equations ?  
Solve :

$$\frac{x-y}{x+3} = \frac{y-1}{4} \text{ and } \frac{4x-5y}{7} = x-7.$$

- (b) Find the equilibrium price and quantity of demand and supply laws given as follows :  
 $3p + 2q = 16, 5p - 3q = 14.$
- (c) What are quadratic equations ? Solve :  
 $(x+2)(x-5)(x-6)(x+6). \quad 10+5+5=20$
2. (a) Differentiate between A.P series and G.P series.  
(b) How many terms of the series  $9 + 12 + 15 \dots$  will make the sum 225 ?  
(c) The third term of a GP is 4.5 and the ninth term is 16.2. Find the first term and the common ratio.  
(d) If you save 1 paise today, 2 paise next day and 3 paise the succeeding day and so on, what will be your savings in 365 days ?  $5+5+5=20$

### SECTION—B

3. (a) Derive the equation of straight line passing a given point  $(x_1, y_1)$  and whose slope is  $m$ . Find the equation of straight line passing through the point  $(4, 5)$  and make an intercept of 3 units with  $x$ -axis.
- (b) (i) What is the symmetric difference of two sets ? If  $A = \{1, 3, 7, 4\}$ ,  $B = \{6, 7, 8, 9\}$ . Find  $A \Delta B$ .
- (ii) Discuss :
- (1) union of two sets and
  - (2) complement of two sets with the help of example.
- (c) Explain the concept of permutation with the help of example.  $5+10+5=20$
4. (a) Find the equation of straight line passing through the point  $(-1, 3)$  and has the slope 2.
- (b) Find the equation of straight line which cuts off intercept 4 and 5 on the  $x$ -axis and  $y$ -axis respectively.
- (c) Discuss the intersection of two sets and difference of two sets with the help of examples.
- (d) Explain the concept of combination with the help of an example.  $5+5+5+5=20$

### SECTION—C

5. (a) Explain the term function. Differentiate between explicit and implicit functions.
- (b) Evaluate  $\lim_{x \rightarrow 2} \frac{x^3 - 8}{x - 2}$  by method of substitution.
- (c) Write and interpret the supply function with its specific form.
- (d) Differentiate  $x^2$  by using ab-initio principle.  
5+5+5+5=20
6. (a) Explain the graph of linear and quadratic functions with the help of examples.
- (b) Differentiate between constant and variable.
- (c) Show that  $f(x) = \frac{x^2 + 1}{x - 1}$  is continuous at  $x = 2$ .
- (d) Differentiate w.r.t.  $x$  from first principle :  
 $y = 3x + 4$ . 5+5+5+5=20

### SECTION—D

7. (a) Discuss the power function and quotient rules of differentiation.
- (b) Find  $\frac{dy}{dx}$  when  $x = \frac{3at}{1+t^3}$ ,  $y = \frac{3at^2}{1+t^3}$ .
- (c) Differentiate w.r.t.  $x$  :  $y = \frac{\log x}{x}$
- (d) The demand curve of monopolist is given by  $x = 100 - 4p$ . Find TR, AR and MR.  
5+5+5+5=20

8. (a) Find  $dy/dx$  of the given function :

$$x^2 + 2xy + y^2 = 4.$$

(b) Find  $dy/dx$  ;  $y = \frac{3}{4 + 6e^{3x}}$ .

- (c) Discuss the sum and product rules of differentiation.

- (d) Give the demand function  $q = 100 - 2p - 2p^2$ . Calculate the price elasticity of demand when  $p = 10$ . 5+5+4+6=20